

with(*plots*):

$$f := (x, y) \rightarrow \frac{\cos^2(\text{sqrt}(x^2 + y^2))}{\text{sqrt}(x^2 + y^2 + 1)};$$

$$(x, y) \rightarrow \frac{\cos(\sqrt{x^2 + y^2})^2}{\sqrt{x^2 + y^2 + 1}} \quad (1)$$

x- and y-derivatives of f are denoted by g and h here:

g := *unapply*(*diff*(*f*(*x*, *y*), *x*), [*x*, *y*]);

$$(x, y) \rightarrow -\frac{2 \cos(\sqrt{x^2 + y^2}) \sin(\sqrt{x^2 + y^2}) x}{\sqrt{x^2 + y^2 + 1} \sqrt{x^2 + y^2}} - \frac{\cos(\sqrt{x^2 + y^2})^2 x}{(x^2 + y^2 + 1)^{(3/2)}} \quad (2)$$

h := *unapply*(*diff*(*f*(*x*, *y*), *y*), [*x*, *y*]);

$$(x, y) \rightarrow -\frac{2 \cos(\sqrt{x^2 + y^2}) \sin(\sqrt{x^2 + y^2}) y}{\sqrt{x^2 + y^2 + 1} \sqrt{x^2 + y^2}} - \frac{\cos(\sqrt{x^2 + y^2})^2 y}{(x^2 + y^2 + 1)^{(3/2)}} \quad (3)$$

Linearization of f at (a,b):

$$a := \frac{1}{10}; b := 0;$$

$$L := (x, y) \rightarrow f(a, b) + g(a, b) \cdot (x - a) + h(a, b) \cdot (y - b);$$

$$(x, y) \rightarrow f(a, b) + g(a, b) (x - a) + h(a, b) (y - b) \quad (4)$$

$$\text{plot3d}\left(\{f(x, y), L(x, y)\}, x = -2..2, y = -2..2, \text{transparency} = \frac{3}{10}\right)$$

